Logarithmic and Exponential Equations - Practice (and solutions)

Logarithmic equations can sometimes be solved by exploiting the one-to-one property of logarithmic functions. That is,  $(this=that) \Leftrightarrow \log(this) = \log(that)$ .

For example, if we have  $\log_2(4x - 3) = \log_2 13$  then we can solve this by using the one-to-one property.

$$4x - 3 = 13$$
  
 $4x = 16$   
 $x = 4$ 

Other exponential equations can be solved using logarithms. Using the oneto-one property, if we have this = that then, log(this) = log(that)

For example,

5.  $4^x = 12$ 

$$2^{x} = 7$$
$$\log 2^{x} = \log 7$$
$$x \log 2 = \log 7$$
$$x = \frac{\log 7}{\log 2}$$

Solve each of the following equations.

- 1.  $\log_a(x+4) \log_a(x+2) = \log_a x$  6.  $3^{2x-5} = 13$
- 2.  $\ln(y+2) = \ln(y-7) + \ln 4$  7.  $e^{2-x} = 12$
- 3.  $\ln(x+1) = \ln(x-4)$ 8.  $10e^{3x-7} = 5$
- 4.  $\log q^2 = 1$ 9.  $\ln x - \ln(x+1) = \ln 5$ 
  - 10.  $\log_4(x+3) + \log_4(x-3) = 1$

This instructional aid was prepared by the Tallahassee Community College Learning Commons.

Answers:

1) $x = \frac{-1 + \sqrt{17}}{2}$	6) $x = \frac{1}{2} \left( \frac{\log 13}{\log 3} + 5 \right) = \frac{\log 13}{\log 9} + \frac{5}{2}$
2) $y = 10$	7) $x = 2 - \ln 12$
3) Ø	8) $x = \frac{7 + \ln \frac{1}{2}}{3} = \frac{7 - \ln 2}{3}$
4) $q = \sqrt{10}$	3 3 9) Ø
5) $x = \frac{\log 12}{\log 4}$	10) $x = \pm \sqrt{13}$