## Trigonometry Fundamentals and the Unit Circle

The six trigonometric functions sine, cosine, tangent, cosecant, secant, cotangent are derived from relationships with right triangles. Common values result from two right triangles:
1


$$
\begin{aligned}
& \sin \left(30^{\circ}\right)=\frac{\text { OPP }}{\text { HYP }}=\frac{1}{2} \\
& \cos \left(30^{\circ}\right)=\frac{\text { ADJ }}{\text { HYP }}=\frac{\sqrt{3}}{2} \\
& \tan \left(30^{\circ}\right)=\frac{\text { OPP }}{\text { ADJ }}=\frac{1}{\sqrt{3}}=\frac{\sqrt{3}}{3}
\end{aligned}
$$

(Note: values for $60^{\circ}$ are found similarly.)

1

$$
\begin{aligned}
& \sin \left(45^{\circ}\right)=\frac{\text { OPP }}{\text { HYP }}=\frac{1}{\sqrt{2}}=\frac{\sqrt{2}}{2} \\
& \cos \left(45^{\circ}\right)=\frac{\text { ADJ }}{\text { HYP }}=\frac{1}{\sqrt{2}}=\frac{\sqrt{2}}{2} \\
& \tan \left(45^{\circ}\right)=\frac{\text { OPP }}{\text { ADJ }}=\frac{1}{1}=1
\end{aligned}
$$

"All Students Take Calculus"
"SOH CAH TOA"


ADJ

SOH $\sin \boldsymbol{\theta}=\frac{\mathrm{OPP}}{\mathrm{HYP}}$
$\csc \boldsymbol{\theta}=\frac{\mathrm{HYP}}{\mathrm{OPP}}$
CAH $\quad \cos \boldsymbol{\theta}=\frac{\text { ADJ }}{\text { HYP }} \quad \sec \theta=\frac{\text { HYP }}{\text { ADJ }}$

TOA $\boldsymbol{\operatorname { t a n }} \boldsymbol{\theta}=\frac{\mathrm{OPP}}{\mathrm{ADJ}}$
$\boldsymbol{\operatorname { c o t }} \boldsymbol{\theta}=\frac{\mathrm{ADJ}}{\mathrm{OPP}}$


The Unit Circle - the center at the origin; a radius of 1.
Coordinates of $(\cos \theta, \sin \theta)$


