

## Rules of Divisibility

Divisible by:	Test	Example
<b>2</b>	Last digit is even (=0, 2, 4, 6, or 8)	3,489,076: Last digit = 6 ( <b>even</b> ) $6 = 3 \times 2$
<b>3</b>	<ol style="list-style-type: none"> <li>The sum of the digits of the number is divisible by 3</li> <li>Can repeat until sum is 2-digit number that is/not recognizably divisible by 3</li> </ol>	16,499,205,854,376: $1 + 6 + 4 + 9 + 9 + 2 + 0 + 5$ $+ 8 + 5 + 4 + 3 + 7 + 6 = 69$ $6 + 9 = 15$ $15 = 5 \times 3$
<b>4</b>	<ol style="list-style-type: none"> <li>Last 2 digits are divisible by 4</li> <li>Tens digit is even and the ones digit = 0, 4, or 8</li> <li>Tens digit is odd and the ones digit = 2 or 6</li> </ol>	358,912: <ol style="list-style-type: none"> <li>Last 2 digits = 12 <math>12 = 3 \times 4</math></li> <li>Tens digit = 1, <b>odd</b> &amp; ones digit = 2</li> </ol>
<b>5</b>	Last digit is 5 or 0	3,783,953,495: Last digit = <b>5</b>
<b>6</b>	Divisible by 2 (even) <b>and</b> 3	57,342 Last digit = <b>2</b> (even) <b>and</b> $5 + 7 + 3 + 4 + 2 = 21$ , divisible by 3
<b>7</b>	Double the last digit, then subtract the result from the rest of the digits. Repeat for larger numbers until result is a 2-digit number; 2-digit number is divisible by 7	357: $2 \times 7 = 14$ (double the last digit) $35 - 14 = 21$ (subtract) $21 = 3 \times 7$
<b>8</b>	<ol style="list-style-type: none"> <li>Hundreds digit even: last 2 digits divisible by 8</li> <li>Hundreds digit odd: add 4 to the last 2 digits and sum is divisible by 8</li> <li>Last 3 digits divisible by 8</li> </ol>	986,104: <ol style="list-style-type: none"> <li>Hundreds digit = 1, <b>odd</b> <math>04 + 4 = 8</math></li> <li>Last 3 digits = 104 <math>104 = 13 \times 8</math></li> </ol>
<b>9</b>	The sum of the digits of the number is divisible by 9	24,343,785: $2 + 4 + 3 + 4 + 3 + 7 + 8 + 5 = 36$ $36 = 4 \times 9$
<b>10</b>	Last digit is 0	34,789,013,467,593,487,540: Last digit = <b>0</b>
<b>11</b>	<ol style="list-style-type: none"> <li>Alternately subtract, then add the digits from L to R; the sum is divisible by 11</li> <li>Subtract the last digit from the rest</li> </ol>	918,082: <ol style="list-style-type: none"> <li><math>9 - 1 + 8 - 0 + 8 - 2 = 22</math> <math>22 = 2 \times 11</math></li> </ol> 627: <ol style="list-style-type: none"> <li><math>62 - 7 = 55</math> <math>55 = 5 \times 11</math></li> </ol>

Divisible by:	Test	Example
<b>12</b>	Divisible by <b>3 and 4</b>	324: $3 + 2 + 4 = 9$ , divisible by <b>3 and</b> Last 2 digits = 24, divisible by <b>4</b>
<b>13</b>	Add 4 times the last digit to the rest of the digits. Repeat until sum is/not recognizably divisible by 13	637: $63 + (7 \times 4) = 91$ $9 + (1 \times 4) = \mathbf{13}$
<b>14</b>	Divisible by <b>2 and 7</b>	182: Last digit = 2 (even), divisible by <b>2 and</b> $2 \times 2 = 4$ (double the last digit) $18 - 4 = 14$ , divisible by <b>7</b>
<b>15</b>	Divisible by <b>3 and 5</b>	345: $3 + 4 + 5 = 12$ , divisible by <b>3 and</b> Last digit = 5, divisible by <b>5</b>
<b>16</b>	<ol style="list-style-type: none"> <li>Thousands place even: take the last 3 digits</li> <li>Thousands place odd: add 8 to the last 3 digits</li> <li>With the 3-digit number: multiply hundreds digit by 4, then add the last 2 digits</li> </ol>	254,176: Thousands digit = 4, so 176 $(1 \times 4) + 76 = 80$ $80 = 5 \times \mathbf{16}$ 693,408: Thousands digit = 3, so $408 + 8 = 416$ $(4 \times 4) + 16 = 32$ $32 = 2 \times \mathbf{16}$
<b>17</b>	Subtract 5 times the last digit from the rest	221: $22 - (1 \times 5) = \mathbf{17}$
<b>18</b>	Divisible by <b>2 and 9</b>	35,406: Last digit = 2 (even), divisible by <b>2 and</b> $3 + 5 + 4 + 0 + 6 = 18$ , divisible by <b>9</b>
<b>19</b>	Add twice the last digit to the rest	437: $43 + (7 \times 2) = 57$ $5 + (7 \times 2) = \mathbf{19}$
<b>20</b>	Divisible by 10 and the tens digit is even	360: Last digit = <b>0 and</b> tens digit = 6 is <b>even</b>
<b>25</b>	Last 2 digits are 25, 50, or 75	895,438,675: Last 2 digits = <b>75</b> 7,325: Last 2 digits = <b>25</b>
<b>50</b>	Last 2 digits are 50 or 00	686,352,400: Last 2 digits = <b>00</b> 327,950: Last 2 digits = <b>50</b>