Simplifying Variable Expressions By Combining Like Terms

Like terms are terms where the variable parts are identical. This means that the term must have the same letters and that the exponents, if any, must be the same.

- $3x$ and $5x$ are like terms.
- $3x^2$ and $5x$ are not like terms.
- $-3y$ and $y$ are like terms.
- $-3y$ and $y^3$ are not like terms.

To combine like terms we must first identify those terms which are alike. We then combine them by adding the numerical coefficients. The variable part stays the same.

If there is no number with the variable, the numerical coefficient is understood to be 1 or $-1$ depending upon the sign in front of the terms.

**EXAMPLE:**

$$-4x + 9x$$

$$= (-4 + 9)x$$  Use the Distributive Property

The Distributive Property has been used to rewrite “negative four times $x$” plus “nine times $x$” as “the sum of negative four and nine” times “$x$”.

$$(-4 + 9)x$$  Add the numerical coefficients

$$= 5x$$

**EXAMPLE:**

$$m - 8m$$  Rewrite subtraction

$$m + (-8m)$$

Use the Distributive Property to rewrite “one times $m$ plus negative eight times $m$” to “the sum of one and negative eight times $m$.”

$$1m + (-8m)$$

$$= [1 + (-8)]m$$  Add the numerical coefficients

$$= -7m$$

Some variable expressions have more than two terms. These expressions will require us to use the Commutative and Associative Properties of Addition. We may also need to use the Inverse Property of Addition and the Addition Property of Zero in some problems.
A shorter method of combining like terms is to recognize that the sign in front of a term is the sign of that term and the operation is understood to be addition.

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EXAMPLE: \[5x - 2y + 3x + 6 - 4y - 9\]

\[5x + 3x - 2y - 4y + 6 - 9\]  
As you rearrange the terms this time, take the sign in front of each term with you without rewriting subtraction.

\[(5 + 3)x + [-2 + (-4)]y + [6 + (-9)]\]  
ADD the coefficients mentally.

\[8x - 6y - 3\]  
The terms of the new polynomial are \(8x\), \(-6y\) and \(-3\). If we put these together we get the polynomial \(8x - 6y - 3\).

NOTE that the sign of each term gives you the addition or subtraction sign between the terms. There must be either a “+” or a “−” between each pair of terms.

EXAMPLE: \[-7x^2 + 3x - 2 - 4x^2 + 12x\]

\[-7x^2 - 4x^2 + 3x + 12x - 2\]  
Rearrange the terms

\[-11x^2 + 15x - 2\]  
Combine the coefficients mentally

EXERCISES  Combine like terms.

1. \(-5x - 3x\)  
2. \(8m^2 - 2m + 6m^2\)  
3. \(4 - 8y + 12 - 4x\)  
4. \(-9x^2 - 2x + 8x^2 + x - 7\)  
5. \(12y^3 - 8y^2 - 9y^3 + 8y^2 - y\)  
6. \(\frac{3}{5}x^2 - \frac{1}{2}x + \frac{2}{3}x^2\)

KEY:  
1. 8x  
2. 14m^2 - 2m  
3. -12x + 16  
4. -x^2 - x - 7  
5. 3y^3 - y  
6. \(\frac{19}{15}x^2 - \frac{1}{2}x\)

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